

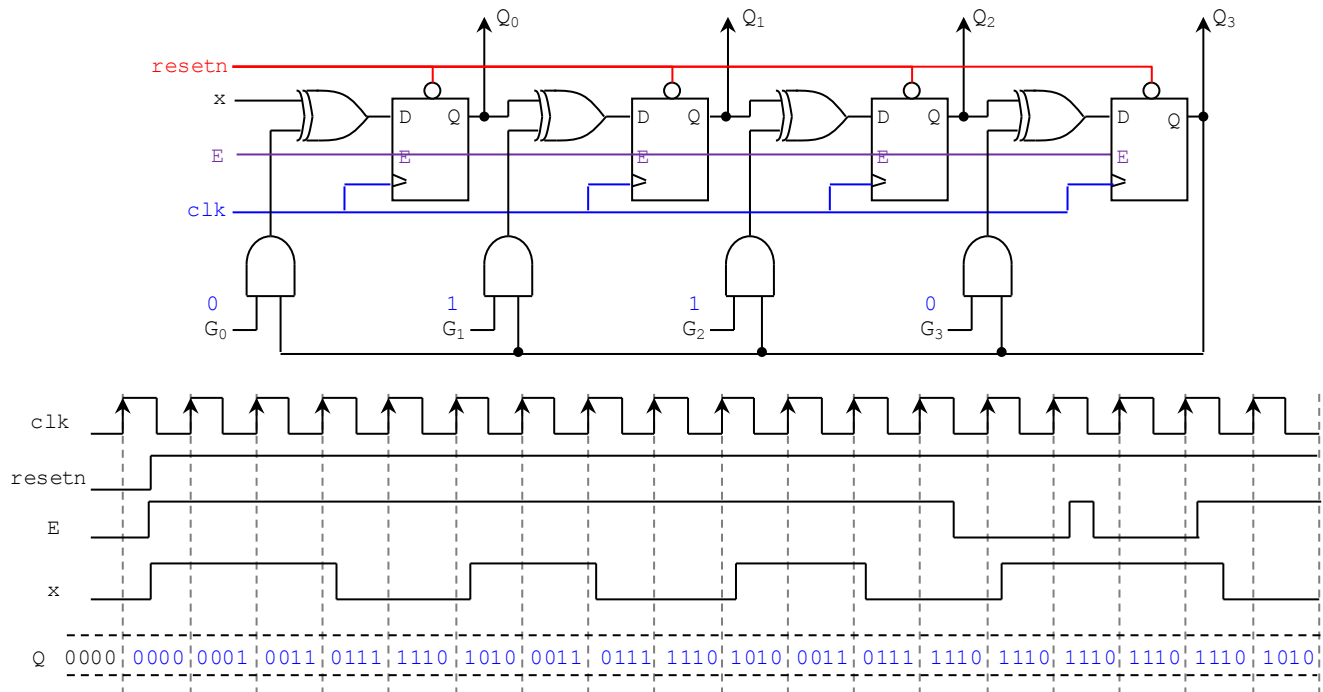
Solutions - Final Exam

(April 21st @ 7:00 pm)

Presentation and clarity are very important! Show your procedure!

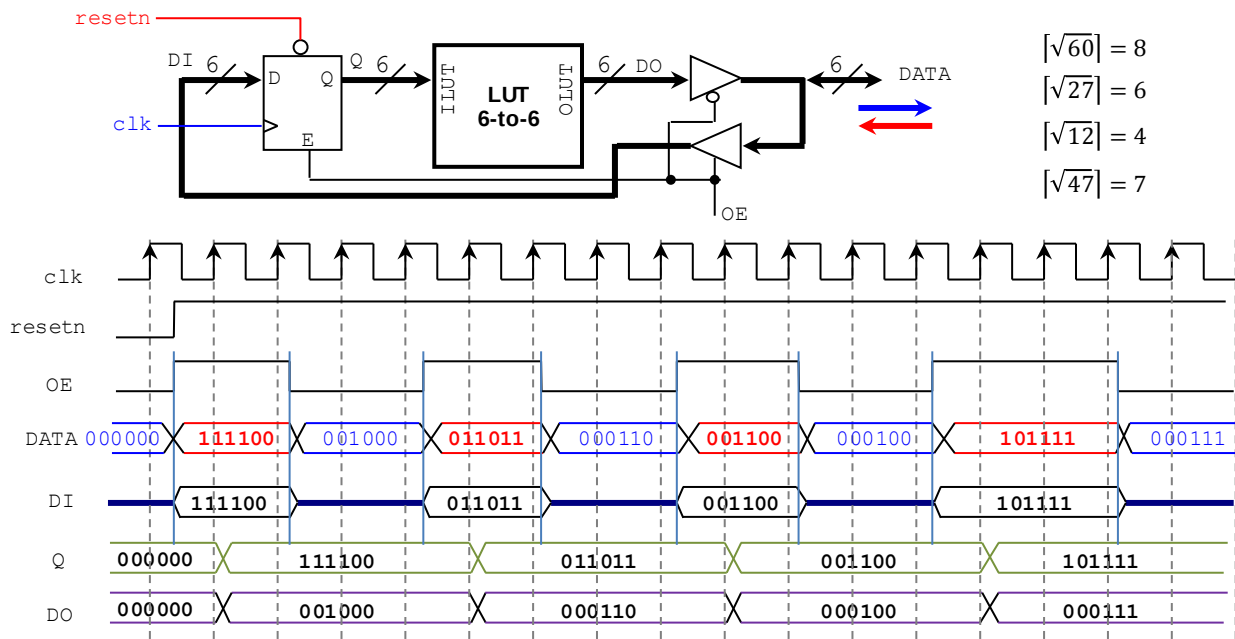
PROBLEM 1 (12 PTS)

- Complete the timing diagram of the following circuit. $G = G_3G_2G_1G_0 = 0110$, $Q = Q_3Q_2Q_1Q_0$



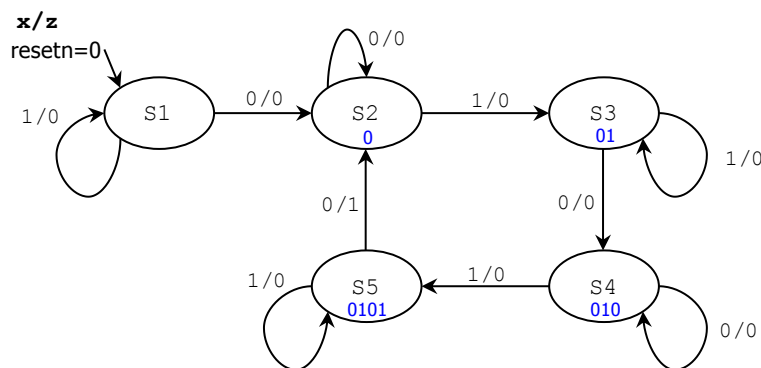
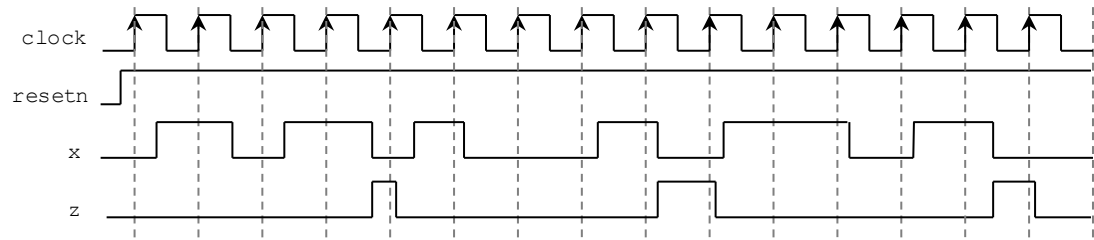
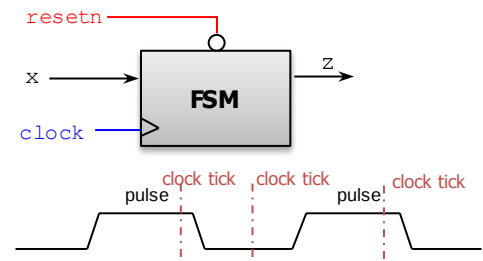
PROBLEM 2 (10 PTS)

- Given the following circuit, complete the timing diagram.
The LUT 6-to-6 implements the following function: $OLUT = \lceil \sqrt{ILUT} \rceil$, where $ILUT$ is a 6-bit unsigned number.
For example $ILUT = 41 (101001_2) \rightarrow OLUT = \lceil \sqrt{41} \rceil = 7 (000111_2)$

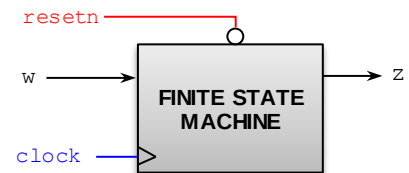


PROBLEM 3 (21 PTS)

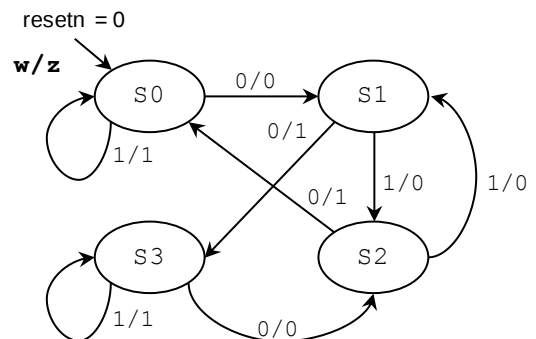
- Two-pulse Detector: The timing diagram shows the behavior of the circuit. The FSM generates $z = 1$ when it detects two pulses. Note how in this design, the output z is 1 as soon as the second $1 \rightarrow 0$ transition is detected. Once the two pulses are detected, the FSM looks for a new pair of pulses. Assumption: For the circuit to detect a '1' or a '0' on x , this value needs to happen when a rising edge occurs. Draw the State Diagram (any representation) of the given FSM (10 pts).



- The following FSM has 4 states, one input w and one output z . (11 pts)
 - ✓ The excitation equations are given by:
 - $Q_1(t+1) \leftarrow Q_0(t)$
 - $Q_0(t+1) \leftarrow Q_1(t) \oplus \bar{w}$
 - ✓ The output equation is given by: $z = Q_1(t) \oplus Q_0(t) \oplus w$

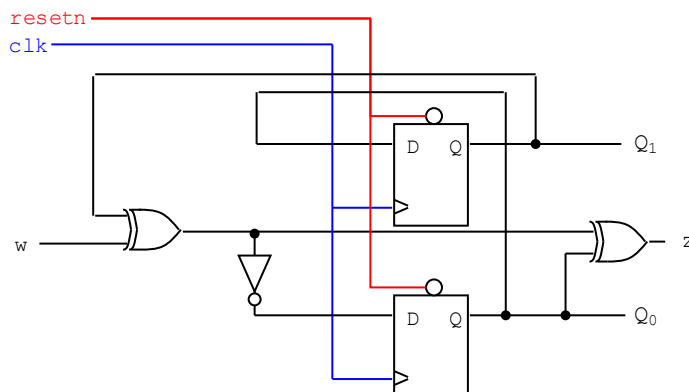


PRESENT STATE			NEXTSTATE		
w	$Q_1Q_0(t)$		$Q_1Q_0(t+1)$	z	
0	0 0		0 1	0	
0	0 1		1 1	1	
0	1 0		0 0	1	
0	1 1		1 0	0	
1	0 0		0 0	1	
1	0 1		1 0	0	
1	1 0		0 1	0	
1	1 1		1 1	1	



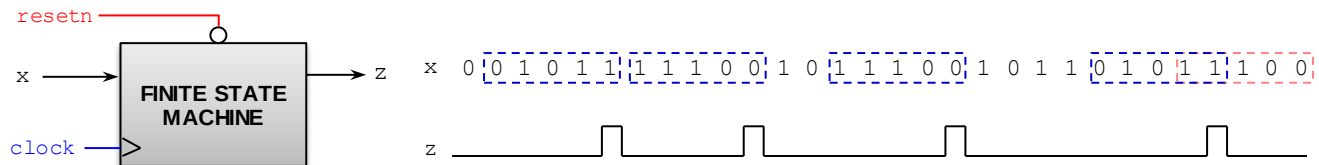
State Assignment:

S0: Q=00 S1: Q=01
S2: Q=10 S3: Q=11

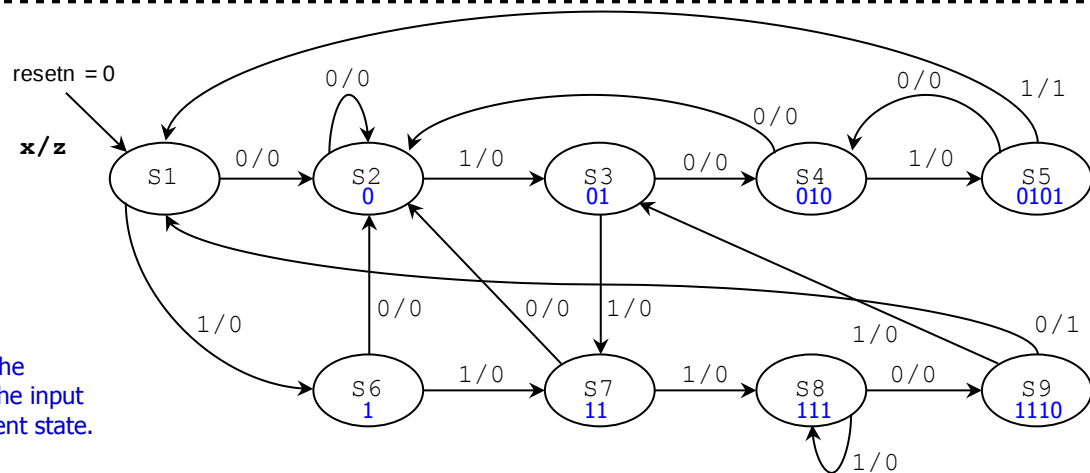


PROBLEM 4 (11 PTS)

- Sequence detector: This FSM has to generate $z = 1$ when it detects the sequence 01011 or 11100. Once the sequence is detected, the circuit looks for a new sequence. Note that once we start detecting a sequence, we prioritize the sequence that we have over the other (e.g.: last sequence inside a dotted red rectangle is not considered).



- ✓ Draw the State Diagram (any representation) and provide the State Table of this circuit with input x and output z . Is this a Mealy or a Moore machine? Why?



This is a Mealy FSM. The output z depends on the input as well as on the present state.

* Excitation Table shown only for reference.

State Assignment:

S1: Q=0000 S2: Q=0001
S3: Q=0010 S4: Q=0011
S5: Q=0100 S6: Q=0101
S7: Q=0110 S8: Q=0111
S9: Q=1000

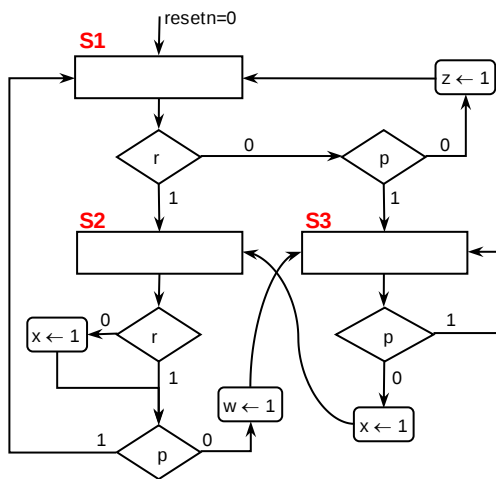
PRESENT STATE		NEXT STATE		z		PRESENT STATE					NEXT STATE					z	
						x	Q ₃	Q ₂	Q ₁	Q ₀ (t)	x	Q ₃	Q ₂	Q ₁	Q ₀ (t+1)		
0	S1	S2	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0
0	S2	S2	0	0	0	0	0	0	0	1	0	0	0	0	1	0	0
0	S3	S4	0	0	0	0	0	0	1	0	0	0	0	1	1	0	0
0	S4	S2	0	0	0	0	0	0	1	1	0	0	0	0	1	0	0
0	S5	S4	0	0	0	0	0	1	0	0	0	0	0	1	1	0	0
0	S6	S2	0	0	0	0	0	1	0	1	0	0	0	0	1	0	0
0	S7	S2	0	0	0	0	0	1	1	0	0	0	0	0	1	0	0
0	S8	S9	0	0	0	0	0	1	1	1	0	0	0	0	0	0	0
0	S9	S1	1	0	0	0	1	0	0	0	0	1	0	0	0	0	1
1	S1	S6	0	0	0	1	0	0	0	1	0	1	0	0	1	X	X
1	S2	S3	0	0	0	1	0	0	1	0	0	1	0	1	0	X	X
1	S3	S7	0	0	0	1	0	0	1	1	0	1	0	1	1	X	X
1	S4	S5	0	0	0	1	0	1	0	0	0	1	1	0	0	X	X
1	S5	S1	1	0	0	1	0	1	0	1	0	1	1	0	1	X	X
1	S6	S7	0	0	0	1	0	1	1	0	0	1	1	1	0	X	X
1	S7	S8	0	0	0	1	0	1	1	1	0	1	1	1	1	X	X
1	S8	S8	0	0	0	1	0	0	0	0	0	1	0	0	0	0	1
1	S9	S3	0	0	0	1	0	0	0	1	0	0	0	1	0	0	0
						1	0	0	1	0	0	1	1	0	0	0	0
						1	0	0	1	1	0	1	0	0	0	0	0
						1	0	1	0	0	0	0	0	0	0	1	0
						1	0	1	0	1	0	1	1	0	0	0	0
						1	0	1	1	0	0	1	1	1	0	0	0
						1	0	1	1	1	0	1	1	1	1	0	0
						1	1	0	0	0	0	0	0	1	0	0	0
						1	1	0	0	1	0	X	X	X	X	X	X
						1	1	0	1	0	0	X	X	X	X	X	X
						1	1	0	1	1	0	X	X	X	X	X	X
						1	1	1	0	0	0	X	X	X	X	X	X
						1	1	1	0	1	0	X	X	X	X	X	X
						1	1	1	1	0	0	X	X	X	X	X	X
						1	1	1	1	1	0	X	X	X	X	X	X

PROBLEM 5 (28 PTS)

- Draw the State Diagram (in ASM form) of the FSM whose VHDL description is shown below. (5 pts)
- Complete the Timing Diagram. (7 pts)
- Provide the State Table and the Excitation Table. Is it a Mealy or a Moore FSM? (6 pts).
- Provide the excitation equations and the Boolean output equations (simplify your circuit: K-maps or Quine-McCluskey).
- Sketch the circuit. (3 pts)

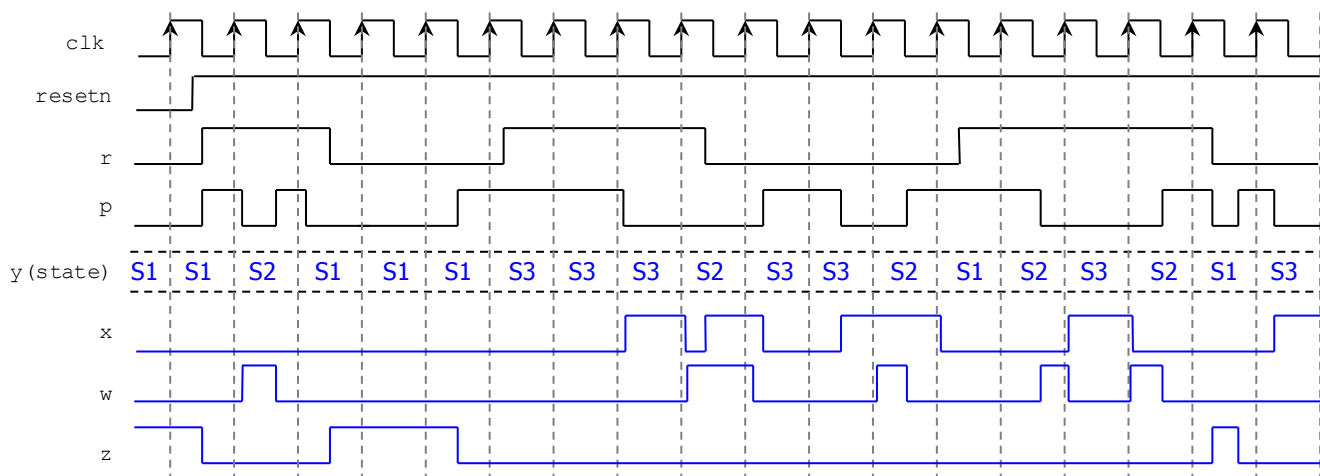
```
library ieee;
use ieee.std_logic_1164.all;

entity myfsm is
    port ( clk, resetn: in std_logic;
          r, p: in std_logic;
          x, w, z: out std_logic);
end myfsm;
```



```
architecture behavioral of myfsm is
    type state is (S1, S2, S3);
    signal y: state;
begin
    Transitions: process (resetn, clk, r, p)
    begin
        if resetn = '0' then y <= S1;
        elsif (clk'event and clk = '1') then
            case y is
                when S1 =>
                    if r = '1' then
                        y <= S2;
                    else
                        if p = '1' then y <= S3; else y <= S1; end if;
                    end if;
                when S2 =>
                    if p = '1' then y <= S1; else y <= S3; end if;
                when S3 =>
                    if p = '1' then y <= S3; else y <= S2; end if;
            end case;
        end if;
    end process;

    Outputs: process (y, r, p)
    begin
        x <= '0'; w <= '0'; z <= '0';
        case y is
            when S1 => if r = '0' then
                            if p = '0' then
                                z <= '1';
                            end if;
                        end if;
            when S2 => if r = '0' then x <= '1'; end if;
                            if p = '0' then w <= '1'; end if;
            when S3 => if p = '0' then x <= '1'; end if;
        end case;
    end process;
end behavioral;
```



State Table and Excitation Table:

PRESENT STATE		NEXT STATE	x w z		
r	p		x	w	z
0	0	S1	0	0	1
0	0	S2	1	1	0
0	0	S3	1	0	0
0	1	S1	0	0	0
0	1	S2	1	0	0
0	1	S3	0	0	0
1	0	S1	0	0	0
1	0	S2	0	1	0
1	0	S3	1	0	0
1	1	S1	0	0	0
1	1	S2	0	0	0
1	1	S3	0	0	0



PRESENT STATE				NEXTSTATE				
r	p	$Q_1Q_0(t)$		$Q_1Q_0(t+1)$		x	w	z
0	0	0	0	0	0	0	0	1
0	0	0	1	1	0	1	1	0
0	0	1	0	0	1	1	0	0
0	0	1	1	X	X	X	X	X
0	1	0	0	1	0	0	0	0
0	1	0	1	0	0	1	0	0
0	1	1	0	1	0	0	0	0
0	1	1	1	X	X	X	X	X
1	0	0	0	0	1	0	0	0
1	0	0	1	1	0	0	1	0
1	0	1	0	0	1	1	0	0
1	0	1	1	X	X	X	X	X
1	1	0	0	0	1	0	0	0
1	1	0	1	0	0	0	0	0
1	1	1	0	1	0	0	0	0
1	1	1	1	X	X	X	X	X

State Assignment:

S1: $Q=00$ S2: $Q=01$

S3: $Q=10$

This is a Mealy FSM. The outputs x, w, z depend on the input as well as on the present state.

Minimization, Excitation equations (including Boolean output equations), and circuit implementation:

$$Q_1(t+1) \leftarrow \bar{r}p\bar{Q}_0(t) + pQ_1(t) + \bar{p}Q_0(t)$$

$$Q_0(t+1) \leftarrow rQ_1(t)Q_0(t) + \bar{p}Q_1(t)$$

$$x = \bar{p}Q_1(t) + \bar{r}Q_0(t)$$

$$w = \bar{p}Q_0(t)$$

$$z = \bar{r}\bar{p}Q_1(t)Q_0(t)$$

$Q_1(t+1)$

rp	00	01	11	10
Q_1Q_0				
00	0	1	0	0
01	1	0	0	1
11	X	X	X	X
10	0	1	1	0

$Q_0(t+1)$

rp	00	01	11	10
Q_1Q_0				
00	0	0	1	1
01	0	0	0	0
11	X	X	X	X
10	1	0	0	1

x

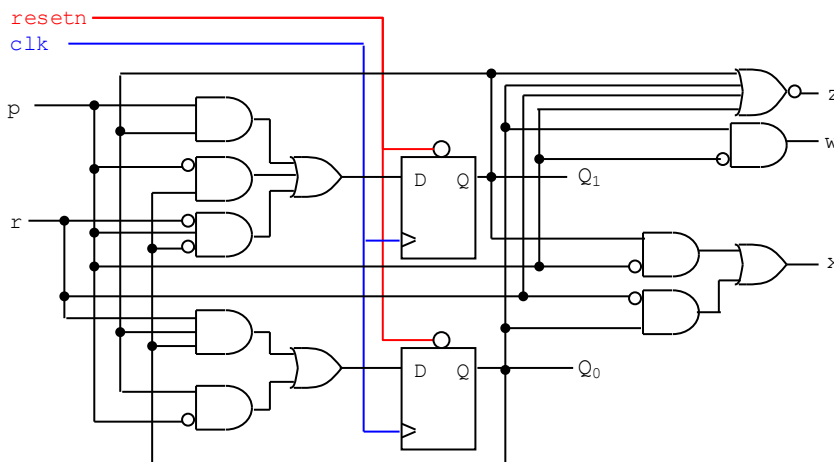
rp	00	01	11	10
Q_1Q_0				
00	0	0	0	0
01	1	1	0	0
11	X	X	X	X
10	1	0	0	1

w

rp	00	01	11	10
Q_1Q_0				
00	0	0	0	0
01	1	0	0	1
11	X	X	X	X
10	0	0	0	0

z

rp	00	01	11	10
Q_1Q_0				
00	1	0	0	0
01	0	0	0	0
11	X	X	X	X
10	0	0	0	0



PROBLEM 6 (18 PTS)

- “Counting 0’s” Circuit: It counts the number of bits in register A that has the value of ‘0’.
The digital system is depicted below: FSM + Datapath. Example: For $n = 8$: if $A = 00110010$, then $C = 0101$.
✓ m -bit counter: If $E = sclr = 1$, the count is initialized to zero. If $E = 1, sclr = 0$, the count is incremented by 1.
✓ Parallel access shift register: If $E = 1, s_l = 1 \rightarrow$ Load. If $E = 1, s_l = 0 \rightarrow$ Shift.
- Complete the timing diagram where $n = 8, m = 4$. A is represented in hexadecimal format, while C is in binary format.

